

Perturbation Theory II

A1.

ADDENDUM

In the lectures we have derived formulae for non-degenerate perturbation theory. The

assumption of a non-degenerate energy spectrum

guarantees that the quantity $\sum_{k \neq n} \frac{\langle \psi_k^{(0)} | \hat{V} | \psi_n^{(0)} \rangle}{E_n^{(0)} - E_k^{(0)}}$

appearing in various equations, is not divergent

which would happen in a degenerate spectrum

because $E_n^{(0)} - E_k^{(0)} = 0$ even if $k \neq n$, for certain values of k and n .

There is, however, an important caveat.

If it so happens that the quantity $\langle \psi_k^{(0)} | \hat{V} | \psi_n^{(0)} \rangle$

$= 0$ for any 2 different degenerate states $|\psi_k^{(0)}\rangle$,

$|\psi_n^{(0)}\rangle$, then in fact the formulae we have

derived are perfectly applicable.

So there are a special class of degenerate models and choice of \hat{V} , where we can still use the formulae we derived.

An example of this is found in EX2. of the final Homework 9.
