

PHY-302

Dr. E. Rizvi

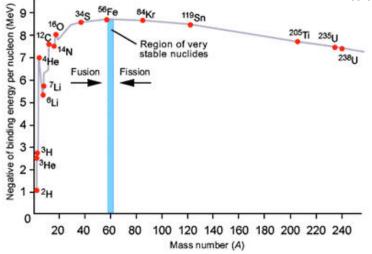
# Lecture 19 - Fusion







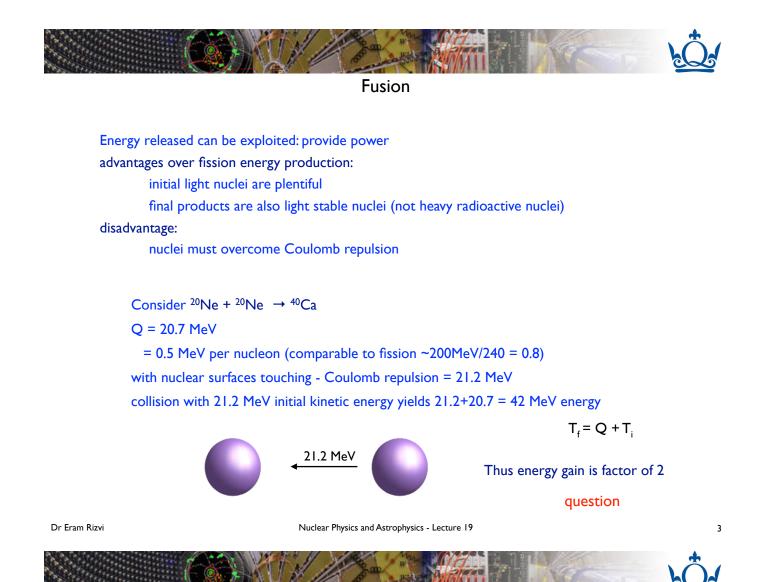
Fusion



Fission: gain binding energy by climbing curve

Fusion: same as fission, start with light nuclei Light nuclei fuse creating heavier element Energy released in process (BE increases) No energy release for A>56 (Fe)

This process occurs in all stars - nucleosynthesis





Collid	ling particle beam experiments can be performed
Not v	iable for energy production - scattering cross section » fusion cross section
Alterr	native approach: heat <sup>20</sup> Ne till thermal energy overcomes Coulomb potential
	each nucleus has <u>on average</u> (3/2) kT thermal kinetic energy:
	need to overcome <u>half</u> Coulomb potential
Know	n as Thermonuclear fusion
Woul	d require temperatures ~ $10^{11}$ K !!! (suns core is ~ $10^7$ K - cannot burn $^{20}$ Ne)
Simple	e picture yields too high critical temp for fusion

Effective temperature for fusion is reduced by accounting for: - QM Tunnelling

- At any temp T, some particles will have more than (3/2)kT energy fraction of particles at high energy for a given temp given by Maxwell-Boltzmann distribution



A basic fusion process is

$$^{2}H + ^{2}H \rightarrow ^{4}He + \gamma$$

Q > energy to separate n or p More likely process is:

$$^{2}H + \ ^{2}H \rightarrow \ ^{3}He + n$$
 Q= 3.3 MeV  
 $^{2}H + \ ^{2}H \rightarrow \ ^{3}H + p$  Q= 4.0 MeV

D-D deuterium-deuterium reaction

More stable final state = more energy release

Expect  ${}^{4}$ He production to have large Q - very stable

$$^{2}H+~^{3}H
ightarrow~^{4}He+n$$
  $\,$  Q= 17.6 MeV

D-T deuterium-tritium reaction

- Coulomb barrier in D-T is same as that of D-D reactions
- Neglecting initial kinetic energies final neutron emerges with 14.1 MeV
- Source of fast neutrons
- This reaction chosen for fusion reactors large energy release
- But: difficult to extract energy from neutron
- Fission: neutrons carry small fraction of energy

easier to extract energy from fission fragments

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### **Fusion Characteristics**

Initial kinetic energies for most fusion processes are small w.r.t. energy release Temp in sun  ${\sim}10^7$  -  $10^8~K$ 

average kinetic energy

$$= (3/2) \cdot 8.6 \times 10^{-8} \cdot 10^{7}$$

= I keV

= (3/2)kT

Typically thermal KE ~1-10 keV i.e.  $T_{initial} \approx 0$  compared to Q ~ 17 MeV !!!

$$Q = \sum_{i} m_{i} + \sum_{f} m_{f}$$
  
=  $T_{final} - T_{initial}$   
Here T means kinetic energy (not temp.)  
apologies for confusing notation!

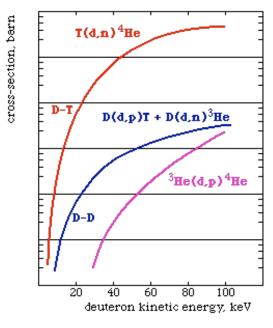
Thus neglecting the initial (thermal) kinetic energy:

 $Q_{fusion} - T_{final}$ 

The lighter particle takes the largest share of the energy



#### Simplified calculations yields this energy dependence of cross section



All fusion cross sections increase as T increases (temp, T ~ deuteron kinetic energy)

D-T reaction has highest cross section for all T

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#### **Fusion Reaction Rate**

Reaction rate =  $\sigma$ .v for a fixed velocity v of nuclei

In thermonuclear fusion reactions particles have Maxwell-Boltzmann velocity distribution

i.e. velocity is not one fixed value. At any temp T, velocity distribution of nuclei is:

$$n(v) \propto e^{-mv^2/2kT}$$

 $n(v) \cdot v^2 \cdot dv$  = relative probability to find particle in range v and v+dv for particles in thermal equilibrium at temperature T

$$\sigma \propto rac{1}{v^2} e^{-2G}$$

Averaging over all velocities 
$$\langle \sigma v 
angle = \int_0^\infty rac{1}{v} \cdot e^{-2G} \cdot e^{-mv^2/2kT} v^2 dv$$

or energies 
$$=\int_0^\infty e^{-2G}\cdot e^{-E/kT}dE$$

Tunnelling barrier penetration probability



At low E: Little overlap between n(E) and  $\sigma.v : \langle \sigma.v \rangle$  average is low At very high E: Maxwell distribution has small area:  $\langle \sigma.v \rangle$  average is low At intermediate E:  $\langle \sigma.v \rangle$  rises to a maximum For 1-10 keV region (T~10<sup>7</sup>-10<sup>8</sup> K) D-T reaction is favoured n(E)  $\sigma.v$ Critical temp for fusion is reduced: - some particles have v. high energy in the Maxwell-Boltzmann dist. - tunnelling of nuclei through Coulomb barrier

Note: A complete calculation would take into account that D and T are different species

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Fusion process powers the sun Occurs at very rapid rate Constant energy output ~ 10<sup>9</sup> years Basic process is fusion of hydrogen into helium In sun: Hydrogen most abundant ~ 90% Helium ~ 9% other atoms < 1% Consider only 2 particle collisions...

Solar fusion is a 3 step process, starting with proton fusion

 ${}^{1}H + {}^{1}H \rightarrow {}^{2}H + e^{+} + \nu_{e}$  Q=1.44 MeV

Note: <sup>2</sup>He production does not occur - pp bound state does not occur! Process occurs with  $\beta^+$  decay (proton converts to neutron)



## Solar Fusion

This is a weak interaction - very small cross section very low probability of occurring occurs via exchange of heavy W boson (mass ~ 80,000 MeV/c<sup>2</sup>)

- For solar temps  $(10^6-10^7 \text{ K})$  small cross section is partially compensated by small Coulomb repulsion
- Nevertheless reaction rate is  $\sim 10^{-18} \text{ s}^{-1}$  per proton
- Solar fusion continues due to enormous number of protons  $\sim 10^{56}$
- Due to low cross section this step in solar cycle known as 'bottleneck' slowest / least probable step in cycle

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Once <sup>2</sup>H has formed then it is easy to form <sup>3</sup>He

$$^{2}H+~^{1}H
ightarrow~^{3}He+\gamma$$
 Q=5.49 MeV

question

П

D-D reaction is very unlikely to occur: very few produced, many more p<sup>+</sup>'s around Deuterons are therefore quickly 'eaten' to produce <sup>3</sup>He  $^{3}He + {}^{1}H \rightarrow {}^{4}Li$  reactions do not occur as <sup>4</sup>Li has no bound state  $^{3}He + {}^{2}H$  reactions do not occur due to lack of deuterons Thus <sup>3</sup>He waits for the reaction:

$$^{3}He + ~^{3}He \rightarrow ~^{4}He + ~2^{1}H\gamma$$
 Q=12.68 MeV



# Proton-proton Cycle

Three steps known as proton-proton (or pp) cycle Net reaction is:

$$4^{1}H \rightarrow {}^{4}He + 2e^{+} + 2\nu_{e} + 2\gamma$$
 Q=26.7 MeV

Not all energy is converted to solar radiation: neutrinos escape and cause no heating of sun

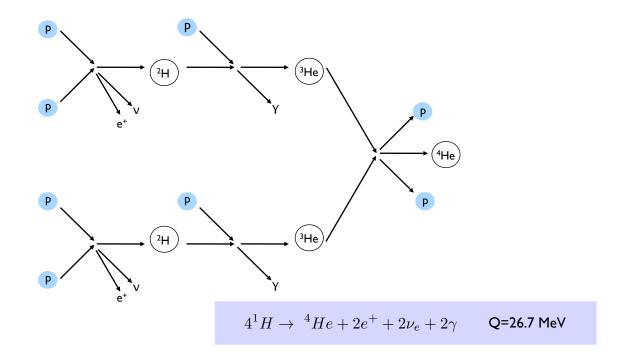
- Measuring neutrino energy spectrum tells us of relative contribution of each process
- Neutrinos escape sun immediately
- Provides us with insight into reactions in core of sun!

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Proton-proton Cycle



13



#### Summary

Fusion process produces heavier nuclei from lighter ones Nuclei need to overcome Coulomb barrier

- achieved at high temp through thermal kinetic energy
- QM tunnelling reduces effective temp for fusion
- high energy tail of Maxwell-Boltzmann spectrum allows drop in temp

Responsible for stellar burning pp cycle dominates solar fusion in our sun

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