

## Energy from Fusion

Carbon-free.

Energy release  $\sim 10^6$  times greater than chemical reaction (similar to fission).

Basic fuel: Deuterium (D), Lithium (Li)

High energy density: 100 g of D and 150 g of tritium (T) required to produce  $\sim 1$  GW for 1 year (same energy content as one Tonne of oil)

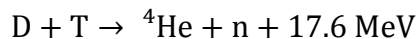
Waste level much lower than fission.

D:  $35 \text{ gm}^{-3}$  in seawater, cost  $\sim \text{£}0.6/\text{g}$

Li reserves  $\sim 10^6$  Tonnes (enough for 10 TWyears for  $\sim 1000$  years)

### D-T fusion

Fusion of deuterium ( $\text{D} \equiv {}^2\text{H}$ ) and tritium ( $\text{T} \equiv {}^3\text{H}$ ) releases 17.6 MeV:



The released energy is shared by the  ${}^4\text{He}$  ( $\alpha$ -particle, 3.5 MeV) and the neutron, n (14.1 MeV)

Deuteron = nucleus of deuterium

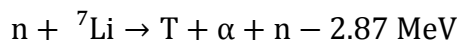
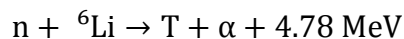
Triton = nucleus of tritium

Need  $10^8$  °C for deuteron and triton fusion to occur at a sufficient rate. Matter is a **plasma** (gas of charged particles with long-range collective effects) in this temperature regime.

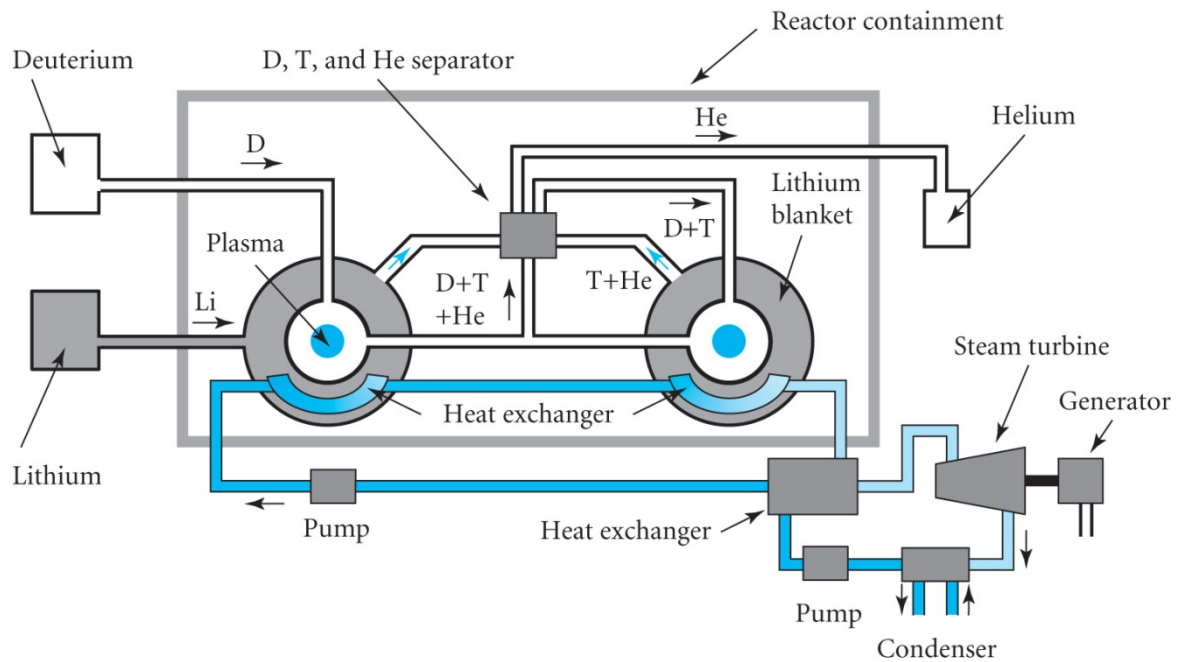
$\alpha$ -particles produced by the D-T reaction provide a source of heat to maintain  $10^8$  °C in the plasma.

Plasma losses energy to reactor walls through radiation, particle diffusion, and heat conduction. Need **magnetic** or **inertial confinement** of plasma. P

Energetic neutrons can be stopped by lithium and used as a source of heat for thermal power a station and produce tritium:



Basic fusion reactor:



(From AJ Ch.9)

The 14.1 MeV neutrons pass through reactor wall and stopped by lithium blanket (tritium also produced)

Natural lithium: 7.4%  ${}^6\text{Li}$ , 92.6%  ${}^7\text{Li}$

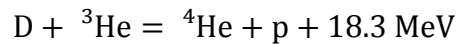
Need tritium breeding ratio (TBR)  $> 1$  for self-sufficiency.

Use the neutron from the  ${}^7\text{Li}$  reaction to increase T production by adding Be or Pb.

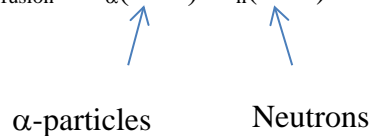
The neutrons from the D-T cycle can produce radioactive nuclei in steel reactor walls. Use 'low activation' steel (recycle after ~50 years), ceramic or fibre composite material.

*Ex. F1* What is the energy produced in one year by the fusion of 100 kg of deuterium and 50 kg of tritium in a reactor?

D+<sup>3</sup>He and D+D reactions:



Fusion power,  $P_{\text{fusion}} = P_{\alpha}(20\%) + P_n(80\%)$



$P_{\alpha}$  heats up plasma

$P_n$  generates heat for heat exchanger so powers the turbine

External power  $P_{\text{ext}}$  may be required in addition to  $P_{\alpha}$  to compensate for losses from plasma (radiation, particle diffusion, heat conduction, bremsstrahlung, synchrotron, radiation emitted from plasma impurities) and optimise plasma conditions.

Power loss,  $P_{\text{loss}} = W / \tau_E$

Where  $W$  = total plasma energy, and

**$\tau_E$  = energy containment time = time for plasma energy to be lost to the walls when plasma is in its operating state but no energy input**

The quality factor  $Q$  is defined as:  $Q = P_{\text{fusion}} / P_{\text{ext}}$

**Break-even:**  $Q = 1$

**Ignition:**  $Q = \infty$  (corresponds to  $P_{\alpha} = P_{\text{loss}}$ , i.e.  $P_{\text{ext}} = 0$ )

The Lawson criterion (AJ Ch.9)

For a 50-50 mixture of D and T,

$$n \tau_E > 12kT / \{ (1 + f_{\alpha}) \langle v \sigma \rangle E_{\text{fusion}} \}$$

$n$  = number of deuterons and tritons per unit volume

$k$  = Boltzmann constant

$T$  = absolute temperature

$f_{\alpha} = P_{\alpha} / P_{\text{fusion}}$

$v$  = nuclear velocity

$\sigma$  = fusion cross-section

$E_{\text{fusion}} = 17.6 \text{ MeV}$

## Charged particle motion in magnetic and electric fields

Lorentz force,  $\mathbf{F} = q\mathbf{E} + q\mathbf{v} \times \mathbf{B}$

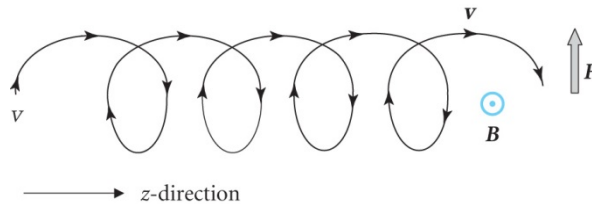
$\mathbf{E}$  = electric field vector

$\mathbf{B}$  = magnetic field vector

$q$  = charge

$\mathbf{v}$  = velocity

When  $\mathbf{E} = 0$  and  $\mathbf{B}$  is uniform, particle gyrates about a magnetic field line with angular velocity  $\omega_c$  (cyclotron frequency), forming a helical path with radius  $\rho$  (Larmor radius):

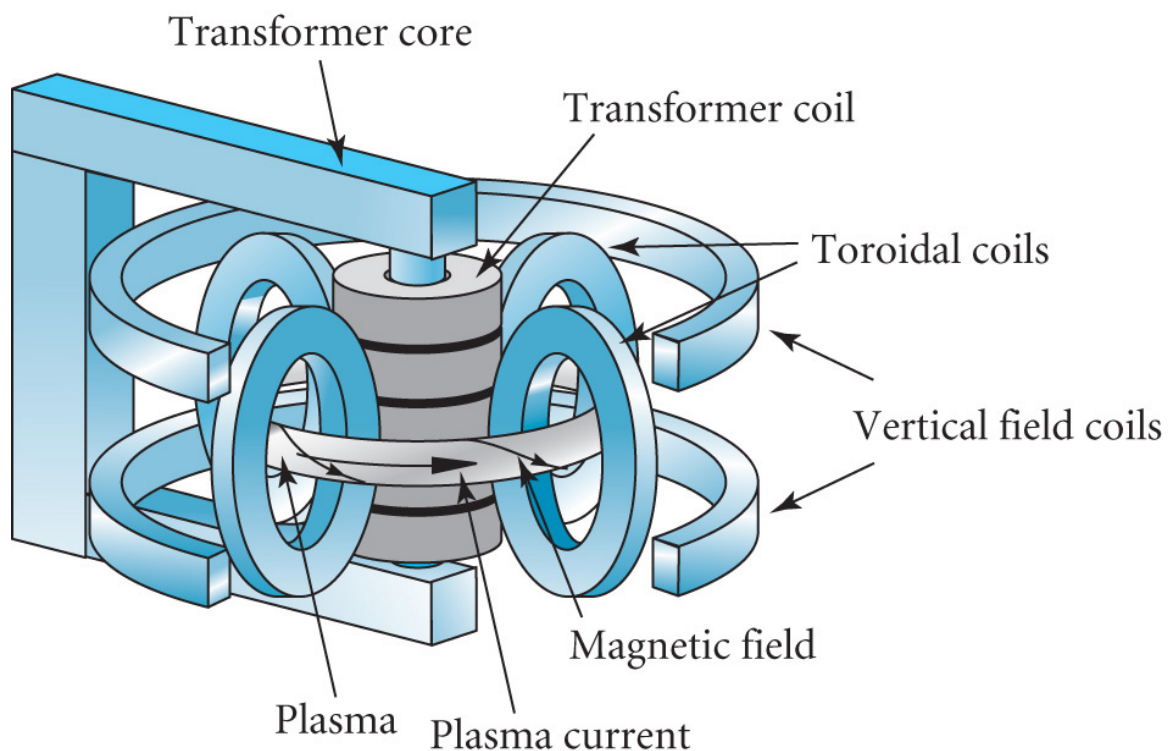


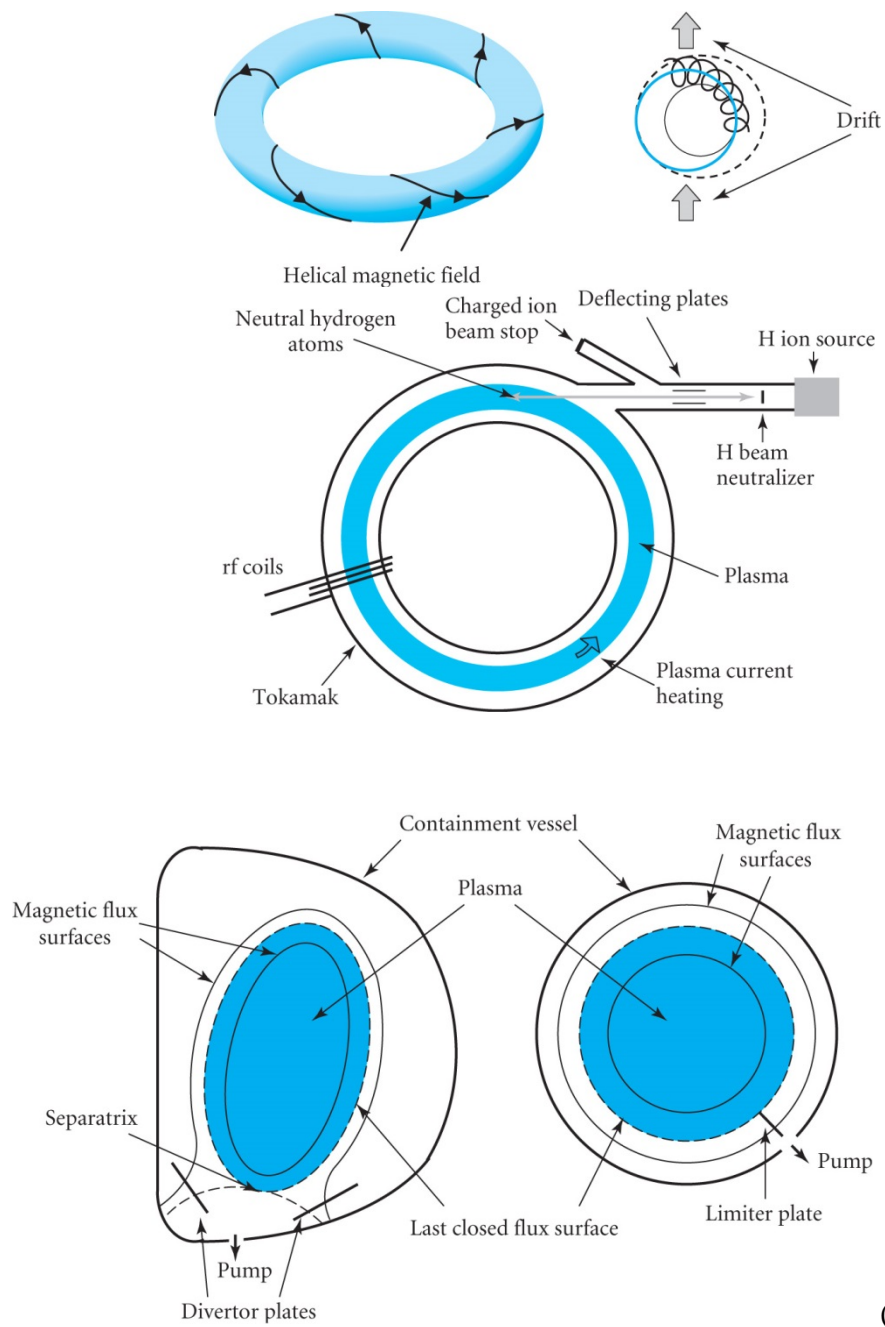
$$\rho = mv_{\perp} / qB,$$

where  $v_{\perp}$  is the component of velocity perpendicular to  $\mathbf{B}$ , and

$$\omega_c = qB/m$$

## The Tokamak





(From AJ Ch 9)

Barriers to progress:

Plasma stability

Ductile to brittle transition in steel subject to high neutron flux